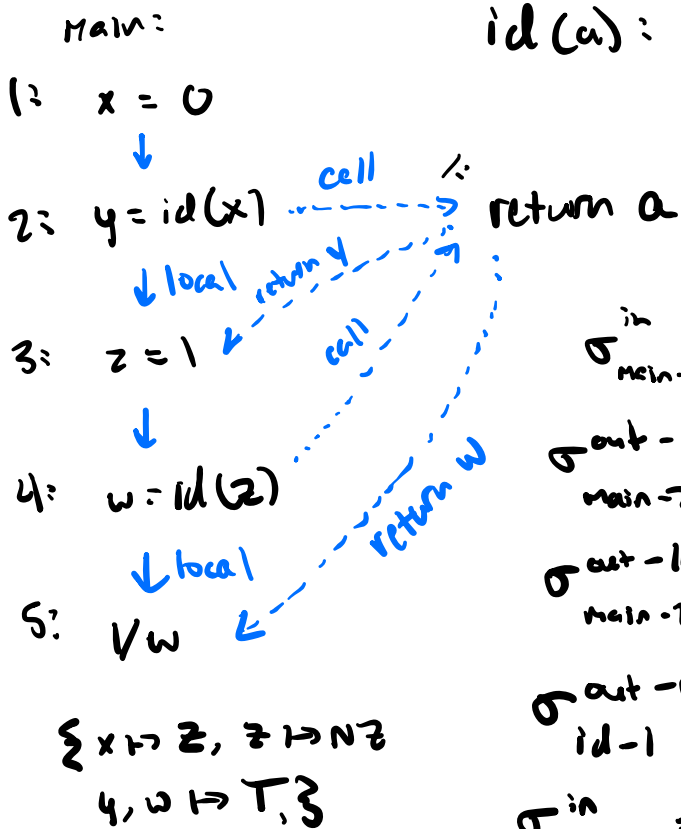


Interprocedural Dataflow

context - insensitive



$$\sigma_{\text{main-4}}^{\text{in}} = \{x, y \mapsto \mathbb{Z}, z \mapsto \mathbb{NZ}\}$$

$$\sigma_{\text{main-4}}^{\text{out-call}} = \{a \mapsto \mathbb{NZ}\}$$

$$\sigma_{\text{main-2}}^{\text{in}} = \{x \mapsto \mathbb{Z}\}$$

$$\sigma_{\text{main-2}}^{\text{out-call}} = \{a \mapsto \mathbb{Z}\}$$

$$\sigma_{\text{main-2}}^{\text{out-local}} = \{x \mapsto \mathbb{Z}\}$$

$$\sigma_{\text{id-1}}^{\text{out-ret-y}} = \{y \mapsto \mathbb{Z}\}$$

$$\sigma_{\text{main-3}}^{\text{in}} = \sigma_{\text{main-2}}^{\text{out-local}} \sqcup \sigma_{\text{id-1}}^{\text{out-ret-y}} = \{x \mapsto \mathbb{Z}, y \mapsto \mathbb{Z}\}$$

$$\sigma_{\text{id-1}}^{\text{in}} = \sigma_{\text{main-2}}^{\text{out-call}} \sqcup$$

$$\sigma_{\text{main-4}}^{\text{out-call}}$$

$$= \{a \mapsto \mathbb{T}\}$$

$$f(x = f(y^*), \sigma)_{\text{local}} = \sigma \setminus \{x\}$$

$$f(x = f(y^*), \sigma)_{\text{call}} = \{f.\text{params}[i] \mapsto \sigma[y_i]\}$$

$$f(\text{return } x, \sigma)_{\text{return } y} = \{y \mapsto \sigma[x]\}$$

Context-sensitive interprocedural analysis

$$f(x = f(y^*), \sigma) =$$

$$\sigma^{\text{start}} = \{f.\text{params}[i] \mapsto \sigma[y_i]\}$$

$$\text{result} = \text{DATAFLOW}(f, \sigma^{\text{start}})$$

$$\text{state} = \bigsqcup_{i \in \text{returns}(f)} \text{result}[i][\text{ret}]$$

$$\sigma[x \mapsto \text{state}]$$

$$f(\text{return } x, \sigma) =$$

$$\sigma[\text{ret} \mapsto \sigma[x]]$$

DATAFLOW

: Function * Domain

$\rightarrow [\text{Domain}]$

$$\sigma^{\text{start}} = \{a \mapsto z\}$$

$$\text{result} = [\{a \mapsto z, \text{ret} \mapsto z\}]$$

$$\text{state} = z$$

$$\sigma[y \mapsto z]$$

$$x = \perp$$

$$y = \text{id}(x)$$

$$z = 1$$

$$n = \text{id}(z)$$

$$1/\perp$$

$$f(x: \text{int})$$

if ...



return x



return $\emptyset$

$$f(z)$$

Information Flow

```
#[secure]
fn passwd() → string {
  input()
}
```

```
fn main() {
  let p = passwd() in
  write_secret(p)
}
```

```
fn write_secret(p: string) {
```

```
  println(p)
```

```
  if p == "..." {
```

```
    println("ok")
```

```
    secret_op();
```

```
  }
```

```
  println("hello")
```

```
}
```

information flow = explicit $\cup$ implicit

data flow
explicit flow

control flow
implicit flow

Data Flows

$\Delta = \{ \text{insecure}, \text{secure} \}$
insecure $\subseteq$ secure

$\sigma \in \{ \text{Var} \mapsto \Delta \}$

$f(x = c, \sigma) = \sigma[x \mapsto \text{insecure}]$

$f(x = f(y), \sigma) = \sigma[x \mapsto \text{secure}]$ if f marked secure
 $= \sigma[x \mapsto \text{secure}]$

$f(x = y \oplus z, \sigma) = \sigma[x \mapsto \sigma[y]] \cup \sigma[z]$

$f(x = y, \sigma) = \sigma[x \mapsto \sigma[y]]$

```
...
↓
if p == "..."
```

```
  ↙ A
  println()
  ↓
  ↘ B
  println()
  ↓
  return
```

Dominance

A

↓

B

↙

C

↓

D

↓

E

Post-dominance:

A postdom B if all paths from exit

A dominates B if all paths from start to B go through A

to B go through A

α is control-dependent on β if:

A) β does not pdom α

B) there exists a path from
to s.t. all C on the path
are pdom by (except ,)

